

# Conflicts and Incentives in Wireless Cooperative Relaying: A Distributed Market Pricing Framework

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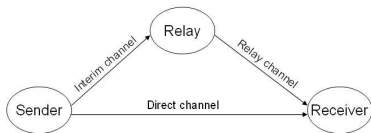
Joint work with Lavy Libman (Univ. Sydney) and Jean Leneutre (Télécom ParisTech):  
submitted to IEEE TPDS

# Outline

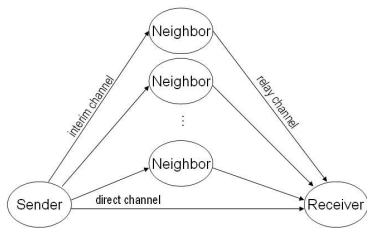
- Cooperative relaying: a brief overview
  - basic concepts
  - difference from traditional approaches
  - sample of some recent work
- The need for game theory and pricing in modelling of cooperative relaying systems
  - conflicts among cooperative relay nodes and flows
- Our work: a distributed market pricing framework
- Conclusion and future directions

# Cooperative Relaying: the Basic Idea

- Transmission from sender to receiver unsuccessful
  - Overheard by relay node
  - Relay node transmits another signal
  - With the new signal, receiver can decode information



**Figure:** Cooperative relaying with one relay node



**Figure:** Cooperative relaying with multiple relay nodes

# Differences from classic approaches

- Classic approaches are **layered**
  - decide about route in advance, other route remains unused
- Single-hop transmission (physical/MAC layer)
  - retransmission by sender only
- Routing via two hops (network layer)
  - direct link unused, even if direct transmission heard by receiver
- Cooperative communication
  - aka cooperative relaying / forwarding / retransmission / ARQ ...
  - Take advantage of wireless medium broadcast nature
  - Potential to combine benefits from both layers **opportunistically**
  - Especially useful for combating volatile nature of links
    - e.g. slow fading at packet time-scale

# Physical-layer strategies

- Relaying by cooperative neighbor
  - amplify-and-forward
  - decode-and-forward
  - coded cooperation (cooperative FEC)
- Single-relay case widely studied in the literature
  - effective channel capacity / BER curves
  - tradeoffs and optimal schemes well-understood

# Cooperation by multiple relays: existing approaches

- Choose one “best” relay
- Multiplex relay transmissions (frequency, code, ...)
  - needs multiple receiver circuits
- Cooperative diversity on physical layer
  - conceptually similar to MIMO
  - taking advantage of spatial diversity
  - need multiple receiver antennas or sophisticated “space-time codes”
  - extensive research in recent years
- Higher layers: variations on **opportunistic routing**
  - packet is broadcast, multiple ACKs returned, then next hop chosen
    - Selection Diversity Forwarding (SDF), Larsson 2001
    - Geographic Random Forwarding (GeRaF), Zorzi et al 2003
  - or implicit coordination by random waiting instead of ACKs
    - Extremely Opportunistic Routing (ExOR), Biswas and Morris 2005

# Summary for now

- Cooperative relaying
  - cross-layer approach (joint PHY/MAC+routing)
  - opportunistic (packet route not determined in advance, may be relayed by multiple nodes)
  - defeats traditional routing in presence of short-term channel losses
- Majority of existing literature: focus on optimization and/or performance bounds of single transmitter/receiver pair
  - no consideration of conflict among multiple flows for same resource pool (cooperative relay nodes)
  - no consideration of possibly selfish relay nodes
  - related work from NUM theory / MANETs inapplicable

# Our work: Background and Motivation

- Most existing solutions focus on optimization perspective
- Conflicts in cooperative relaying
  - Helping one flow means cannot help others
  - Increased interference among flows caused by cooperative relaying
  - More complicated interactions among flows between different source/destination pairs in the presence of cooperative relaying
  - Need distributed mechanisms for efficient allocation of cooperative relay nodes among the heterogeneous flows
- Our work: investigate the conflicts and incentives in cooperative relaying using a distributed market pricing framework



# Related work on applying game theory on distributed mechanism/protocol design in networks

- Apply pricing as a distributed control mechanism to orient the system towards a social optima
  - Network Utility Maximization (NUM) [1]
    - Not applicable in cooperative relaying
    - No clear distinction between “users” and “resources”
- Research on incentives in ad hoc networks: credit-based and reputation-based approach [2]
  - Not applicable in cooperative relaying, either
  - No pre-determined path, each packet may be relayed by multiple nodes
- Market-based frameworks, [3-5]
  - Our work can be viewed as the adaptation of market-based pricing methodology to the cooperative relaying context

# Overview of Our Work

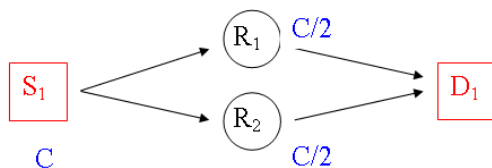
- A market pricing framework to study the conflicts and incentives in cooperative relaying
- Main contributions
  - First pricing framework for cooperative communication
  - Game theoretic analysis on the proposed pricing framework
    - NE structure: existence, uniqueness, convergence, efficiency
    - Competition among source and relay nodes
- Distinctive features of our work from previous research
  - In our work: 2 types of players (the relay nodes and the flow sources), each of which is not only in competition with its peers but also with players of the other type
  - The payment from a flow is shared among all relay nodes successfully participating in the relaying of that flow
    - A node's utility depends not only on prices but also on the strategies of its peers
    - Competition scenario with more complex interactions among players
    - Non-concave utility, needs original study of the equilibrium properties

# Network Model

- We consider a synchronized slotted wireless network consisting of
  - A set  $\mathcal{F}$  of flows
  - $S_f, D_f$ : source and destination of flow  $f$
  - A set  $\mathcal{R}$  of relay nodes
  - Simple memoryless channel model: either good or bad
  - $P_{sn}^f (P_{nd}^f)$ : probability that the channel between  $S_f$  and any relay node (any relay node and  $D_f$ ) is good
- Each relay node can only relay one pkt at a time
- The transmission is successful if at least one relay node successfully relay the packet to its destination

# Proposed Pricing Framework

- Flow sources pay the relay nodes in exchange for their cooperative relaying
- The payment  $C^f$  (per successful pkt) is shared fairly among the relay nodes successfully relaying that pkt to its destination



**Figure:** Illustrating example on the pricing framework

# Game Theoretic Model on the Pricing Framework

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<b>Leaders:</b>	Source nodes (flows)
<b>Followers:</b>	Relay nodes
<b>Strategy:</b>	source node $f$ : payment $C^f$ relay node $i$ : $\mathbf{r}_i = \{r_i^f\}$ where $r_i^f$ : prob. that relay node $i$ helps flow $f$
<b>Payoff:</b>	$U_f$ for source node $f$ , $V_i$ for relay node $i$
<b>Game rule:</b>	The leaders select their strategies by anticipating followers' reaction The followers select their strategy based on knowledge of leaders' strategy.

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- The proposed model can be applied in the following generic scenarios
  - A set of “jobs” compete for the services of a pool of “workers”
  - The jobs set their payment rates, workers are free to choose the job(s)
  - The payment from each job is shared equally among all the workers that completed it successfully

# Utility Functions

- Utility function of flow  $f$ :  $U_f \triangleq u_f(P_{suc}^f) - C^f P_{suc}^f$ 
  - $P_{suc}^f$ : prob. that a pkt of  $f$  successfully arrives at dest.
  - $u_f(P_{suc}^f)$  characterizes the satisfaction level of  $f$  at  $P_{suc}^f$
  - $U_f \triangleq$  benefits - payment to relay nodes
- Utility function of relay  $i$ :  $V_i \triangleq \sum_{f \in \mathcal{F}} C^f K^f r_i^f \sum_{l=0}^{R-1} \frac{P^f(l)}{l+1} - e^f r_i^f$

$$(K^f \triangleq P_{sn}^f P_{nd}^f)$$

- $P^f(l) \triangleq \sum_{\substack{\mathcal{T} \subseteq \mathcal{R} \setminus \{i\} \\ |\mathcal{T}|=l}} \prod_{j_1 \in \mathcal{T}} K^f r_{j_1}^f \prod_{\substack{j_2 \notin \mathcal{T} \\ j_2 \neq i}} (1 - K^f r_{j_2}^f)$ : prob. that there are  $l$

additional nodes beside  $i$  successfully relaying the pkt of  $f$  to its dest.

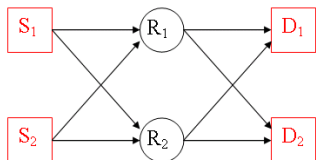
- $\sum_{f \in \mathcal{F}} C^f K^f r_i^f \sum_{l=0}^{R-1} \frac{P^f(l)}{l+1}$ : expected payment from flows
- $e^f$ : transmission cost for relay nodes
- $V_i \triangleq$  share of received payment - cost of cooperation
- $P_{suc}^f = 1 - \prod_{i \in \mathcal{R}} (1 - K^f r_i^f)$

# Solving the Stackelberg Cooperative Relaying Game

- Solve the followers' game
  - For each relay node  $i$ : given the leaders' strategies  $\mathbf{C} = \{C^f\}$  and the strategies of its peers  $\mathbf{r}_{-i} \triangleq \{\mathbf{r}_j, j \neq i\}$ , solve  $\mathbf{r}_i$  maximizing  $V_i$ :  
 $\mathbf{r}_i^*(\mathbf{r}_{-i}, \mathbf{C}) = \operatorname{argmax} V_i(\mathbf{r}_i, \mathbf{r}_{-i}, \mathbf{C})$
  - Results: the followers' equilibrium strategies  $\{\mathbf{r}_i^*(\mathbf{C})\}$
  - Difficulty:  $V_i$  non-concave
- Solve the leaders' game
  - For each flow  $f$ : with the knowledge of  $\mathbf{r}^*(\mathbf{C})$  and given  $\mathbf{C}^{-f}$ , solve  $C^{f*}$  maximizing  $U_f$ :  $C^{f*} = \operatorname{argmax} U_f(C^f, \mathbf{C}^{-f}, \mathbf{r}_i^*(\{C^f, \mathbf{C}^{-f}\}))$
  - Results: the leaders' equilibrium strategies  $\{C^{f*}\}$
- Combine above equilibrium to derive system SNE

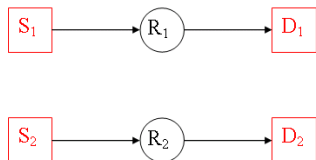
# An Illustrating Example of the Followers' Game

- A system of two flows, two relay nodes with perfectly reliable links:  
 $C^1 = C^2 = 1$ ,  $e^1 = e^2 = 0$ ,  $u_f$  identical for two flows



$$r_1^1=r_2^1=1/2, r_1^2=r_2^2=1/2$$

Symmetrical equilibrium



$$r_1^1=r_2^2=1, r_1^2=r_2^1=0$$

Boundary equilibrium

- 2 kinds of equilibria exist: **symmetrical** and **boundary** equilibrium
  - Symmetrical equilibrium: market competition
  - Boundary equilibrium: market division
  - Continuity property: the symmetrical equilibrium is continuous in  $\mathbf{C}$  while the boundary one is not
- This simple system indicates the followers' game properties in general



# The Followers' Game: Equilibrium Analysis

## Theorem

*For any  $\{C^f\}$ , there exists a unique symmetrical equilibrium in the followers' game.*

## Theorem

*For any  $\{C^f\}$ , there exists at least a boundary equilibrium in the followers' game.*

- Besides, there is no other equilibrium
  - If a strictly interior equilibrium exists in the followers' game, then it is symmetrical.
- The followers' game: 1 symmetrical equilibrium + boundary equilibrium (may not be unique, may coincide with the symmetrical equilibrium)

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# The Leaders' Game: Equilibrium Analysis (1)

## Theorem

*If the followers always respond by playing in their (unique) symmetrical NE, then an equilibrium of the leaders' game (i.e. an SNE of the overall system) exists and is unique.*

## Proof.

Derive the best response function  $B^f(\mathbf{C}^{-f}) = \operatorname{argmax}_{C^f} U_f(C^f, \mathbf{C}^{-f})$  and prove it continuous, bounded and concave in  $\mathbf{C}$ . □

# The Leaders' Game: Equilibrium Analysis (2)

- A boundary equilibrium of followers' game may not lead to SNE for the system
  - In the illustrating example (a system of 2 symmetrical flows with  $e^f = 0, f = 1, 2$ ), the boundary equilibrium for followers' game  $\implies$  no further equilibrium for leaders' game (no SNE of the Stackelberg game)
- Equilibrium structure: substantially different from existing pricing methods

## Theorem

*If the followers always respond by playing in their (unique) symmetrical NE, any asynchronous myopic best-response update for the leader converges to the (unique) equilibrium of the leaders' game.*

# Numerical Studies: SNE Efficiency Analysis

- 2 flows and  $R$  ( $1 \leq R \leq 5$ ) relay nodes
- 2 kinds of utility functions
  - Power-law utility:  $u_f(P_{SUC}^f) = m_f(P_{SUC}^f)^a$ ,  $0 < a \leq 1$
  - Logarithmic utility:  $u_f(P_{SUC}^f) = m_f \log(1 + P_{SUC}^f)$
- For each  $R$ , we run 100 random scenarios with  $m_f \in [1, 100]$ ,  $e^f \in [0, 10]$ ,  $K^f \in [0, 1]$

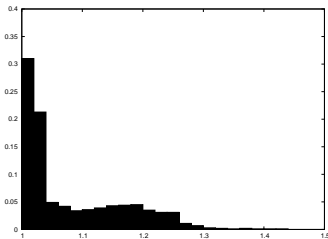
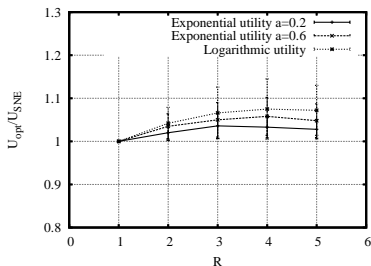


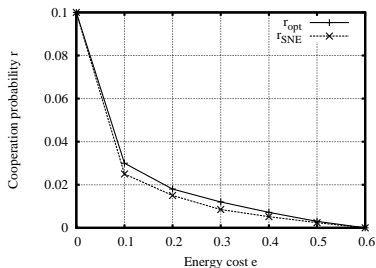
Figure: Histogram of  $U_{SNE}/U_{opt}$  for

Figure: Average ratio between  $U_{opt}$  and  $R = 4$

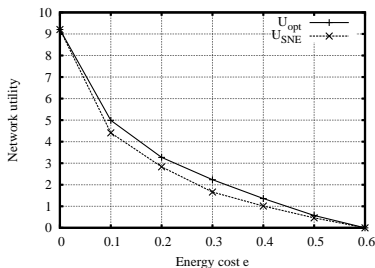
$U_{SNE}$

# Numerical Studies: Large system scenario

- 100 relay nodes and 10 flows with identical parameters of  $K^f = 0.6$ ,  $u_f(P_{SUC}^f) = P_{SUC}^f$ , and  $e^f = e$  for all flows
  - Cooperation probabilities of all relay nodes with all flows are identical ( $r_i^f = r, \forall i \in \mathcal{R}, f \in \mathcal{F}$ ), whether in the (unique) system equilibrium or in the optimal operating point



**Figure:** Cooperation probability as a function of  $e$



**Figure:** Network utility at symmetric optimum and SNE

# Conclusion

- A distributed market pricing framework to study conflicts and incentives in wireless cooperative relaying
  - A game theoretical analysis on the resulting generic Stackelberg game
  - Focus on structural properties on the equilibria and interactions among source and relay nodes
- Perspective
  - Some theoretical problems: analytical bounds for equilibrium efficiency, extensions to the general asymmetrical case
  - Practical mechanism design: how to exchange pricing information among flows and relay nodes, how to enforce payments, etc.



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# Numerical Studies: An asymmetrical scenario

- Asymmetrical relay nodes: heterogeneous  $K^f$  and  $e^f$ 
  - 2 flows and 2 relay nodes, with  $K_1^1 = K_1^2 = 0.8$ ,  $K_2^1 = 0.5$ ,  $K_2^2 = 0.4$ ,  $e^1 = e^2 = 0$ ,  $u_f(P_{SUC}^f) = m_f P_{SUC}^f$ , where  $m_1 = 1$  and  $m_2 = 2$ .
  - Symmetrical equilibrium  $\rightarrow$  interior strategy profile  $\mathbf{r} = \{r_i^f\}$ ,  $0 \leq r_i^f \leq 1$  satisfying  $\frac{\partial V_i}{\partial r_i^f} = 0$ ,  $i, f = 1, 2$  (interior equilibrium)
  - Game dynamics: flows follow best-response update, under the assumption that the followers play an interior equilibrium
- Existence of interior and boundary equilibria in the followers' game and the convergence to the SNE still hold in asymmetrical scenario

